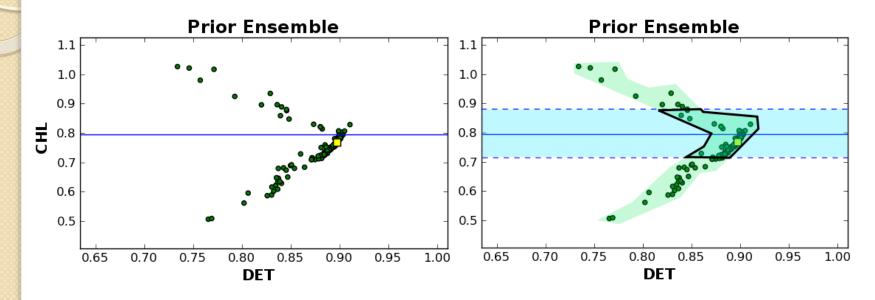


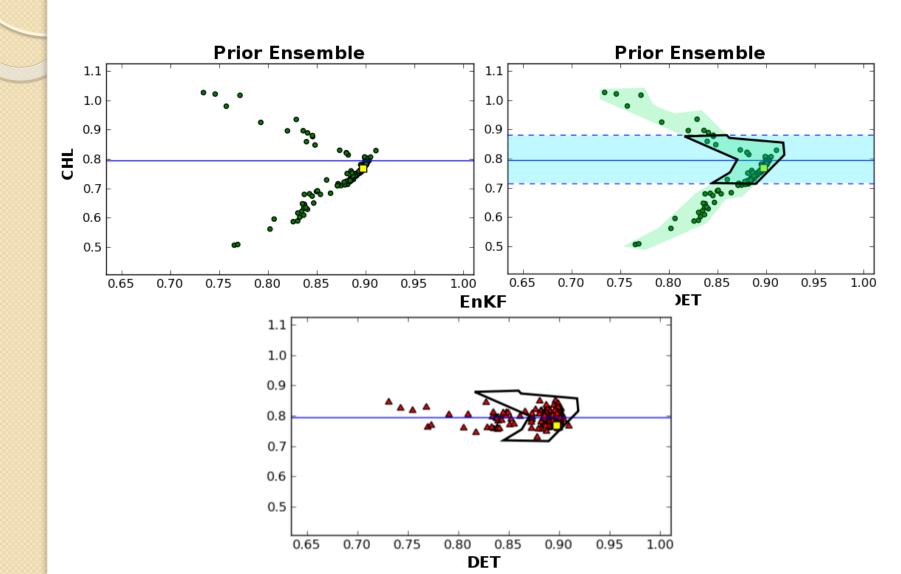
Sammy Metref, Emmanuel Cosme, Pierre Brasseur CNRS-Université Grenoble Alpes, LGGE, Grenoble

Chris Snyder NCAR, Boulder, Co

SANGOMA meeting, April 1-2, 2014, Reading



Ensemble of NATL0.25+BGC simulations (Beal et al., 2010), Gulf Stream station (47W/ 40N). chlorophyll (CHL) / detritus (DET).



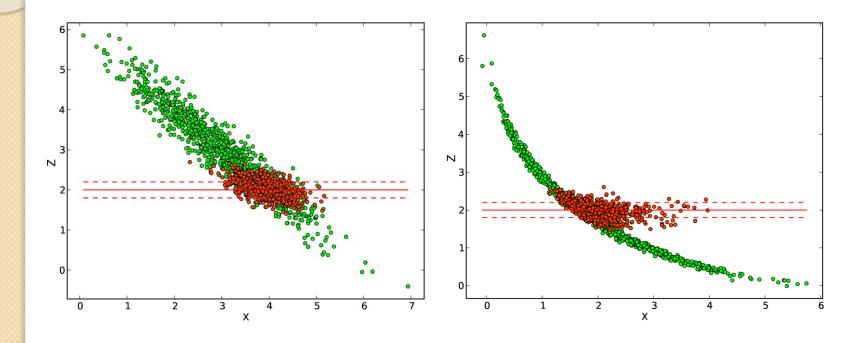
Limitation of the EnKF:

Linear correction for the observed variable:

$$z^a = z^b + K(z^o - z^b)$$

And correction for the **unobserved** variables based on a linear regression with the latter:

$$x^a = x^b + C(z^a - z^b)$$



OK for bivariate Gaussian distributions.

Not OK for bivariate non-Gaussian distributions.

Basic idea of the Multivariate Rank Histogram Filter

For 2 variables x and z, z is observed.

Knothe-Rosenblatt rearrangement of the joint pdf

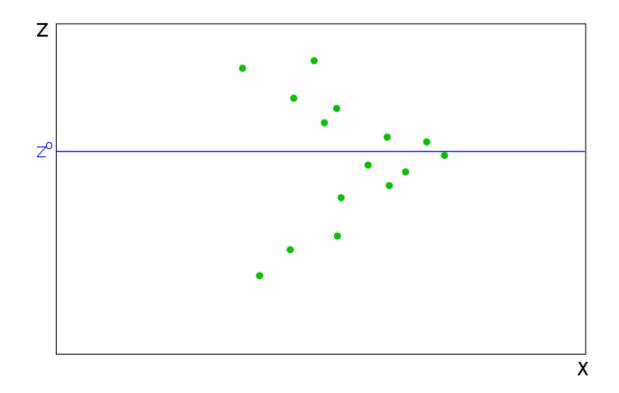
$$p(x,z|z^{o}) = p(z|z^{o})p(x|z,z^{o})$$

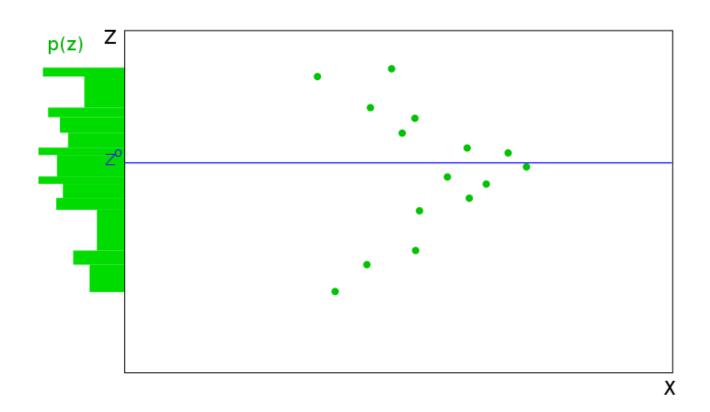
And

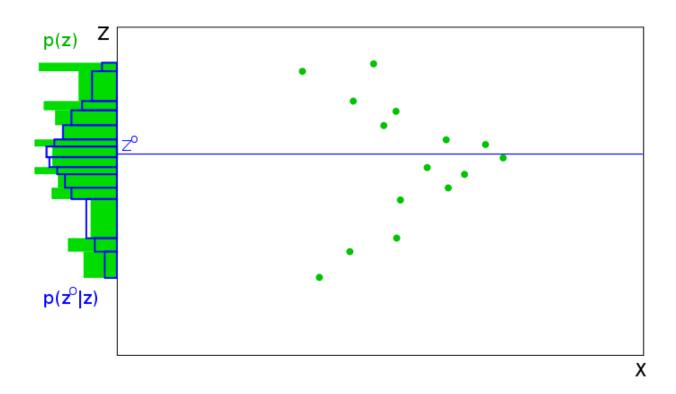
$$p(z|z^o) \propto p(z)p(z^o|z)$$

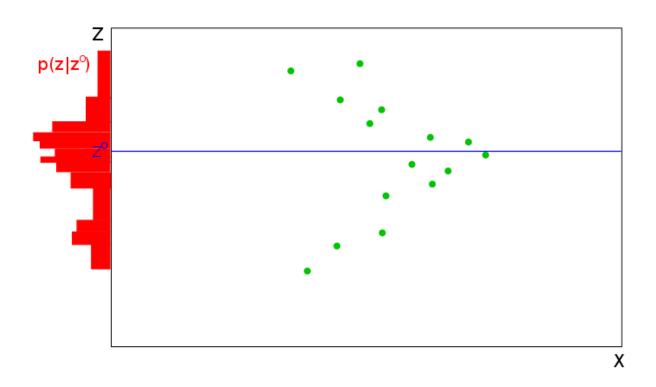
$$p(x|z,z^o) \propto p(x)p(z^a|x)$$

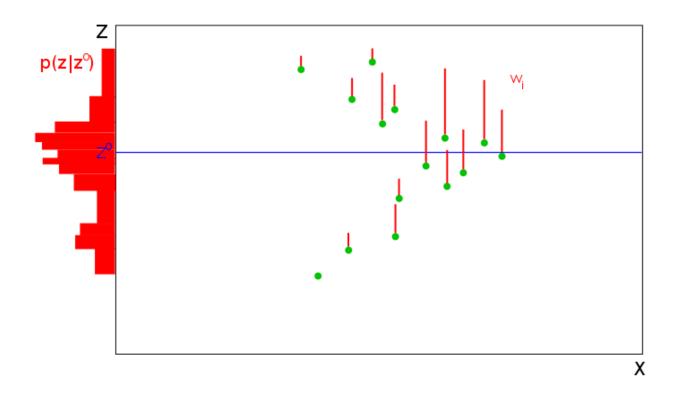
 \rightarrow Sequential computation for z and x (as in the EnKF).

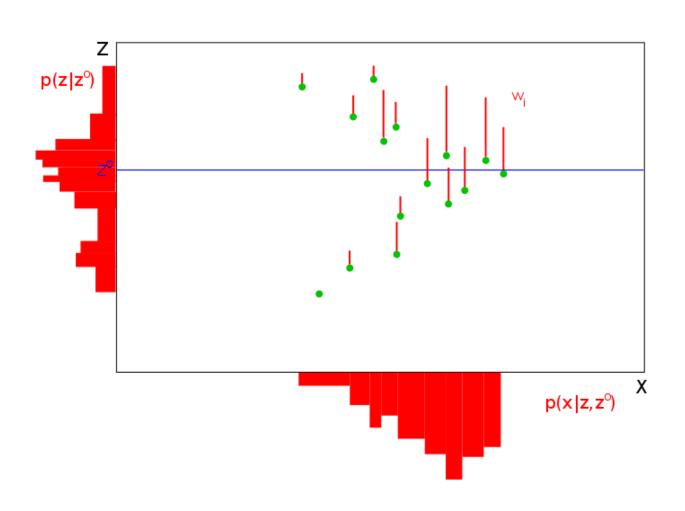


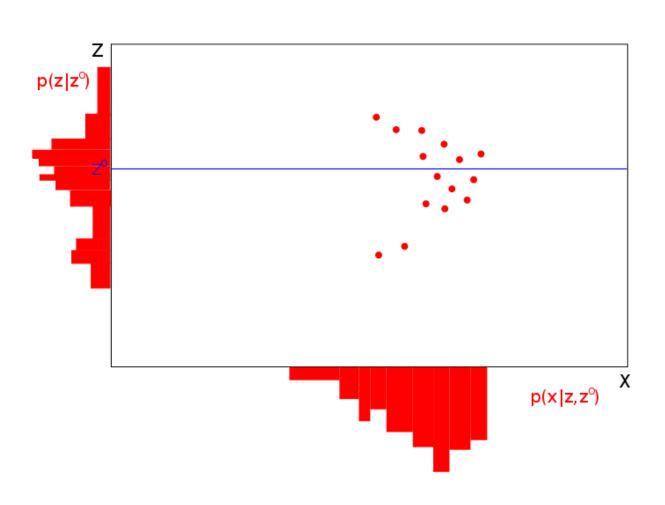












For 3 variables x, y and z, z is observed.

Knothe-Rosenblatt rearrangement of the joint pdf

$$p(x, y, z|z^{o}) = p(z|z^{o})p(x|z, z^{o})p(y|x, z, z^{o})$$

Highly subject to the curse of dimensionality

Unobserved variables are neglected in the conditional statement

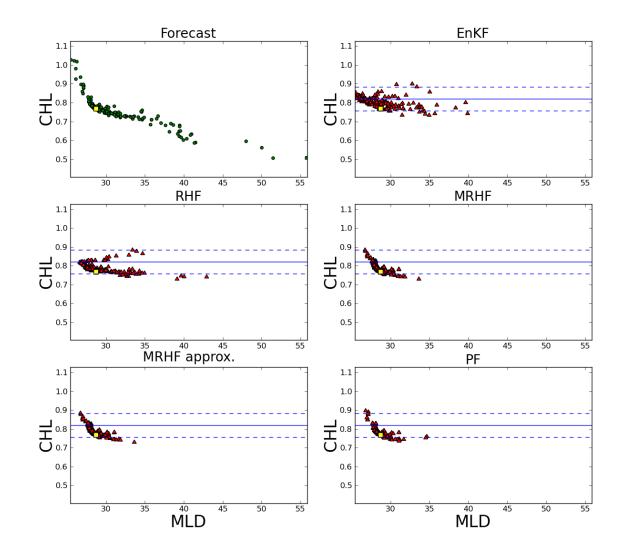
Restriction to the (nonlinear) relation between obs. and each unobs. Variable (like the EnKF)

Analysis illustration

NATL0.25+BGC

Observed: CHL

Unobserved: MLD and DET

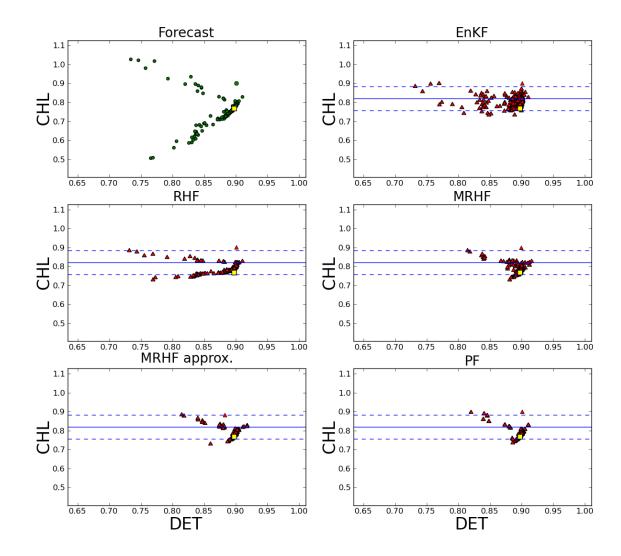


Analysis illustration

NATL0.25+BGC

Observed: CHL

Unobserved: MLD and DET



Analysis illustration

NATL0.25+BGC

Observed: CHL

Unobserved: MLD and DET

